

# **Use It Or Lose It: Efficiency Gains from Wealth Taxation**

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# Taxing Capital

► **Question:** How does **taxing capital income flow** differ from **taxing capital stock**?

■ **Capital income tax:**  $a_{\text{after-tax}} = a + (1 - \tau_k) \cdot r \cdot a$

■ **Wealth tax:**  $a_{\text{after-tax}} = (1 - \tau_a) \cdot a + (1 - \tau_a) \cdot r \cdot a$

► **Standard Answer:** The two taxes are equivalent with  $\tau_a = \frac{r}{1+r} \tau_k \dots$

■ Holds assuming  $r$  is the same for all individuals.

**This Paper:** Take **heterogeneity in  $r$**  seriously and compare forms of **capital taxation**.

► **Short Answer:** The two taxes have very different—even opposite—implications.

# Simple Example

# Return Heterogeneity

- ▶ One-period model.
- ▶ Government taxes to finance  $G = \$50$ . Tax collected end of period.
- ▶ Two brothers, Fredo and Mike, each with \$1000 of wealth.
- ▶ **Key heterogeneity:** investment/entrepreneurial ability.
  - (Fredo) Low ability: earns  $r_f = 0\%$  net return.
  - (Mike) High ability: earns  $r_m = 20\%$  net return.

# Capital Income vs. Wealth Tax

	Capital income tax		Wealth tax	
	$a_{\text{after-tax}} = a + (1 - \tau_k)ra$		$a_{\text{after-tax}} = (1 - \tau_a)a + (1 - \tau_a)ra$	
	Fredo ( $r_f = 0\%$ )	Mike ( $r_m = 20\%$ )	Fredo ( $r_f = 0\%$ )	Mike ( $r_m = 20\%$ )
Wealth	1000	1000	1000	1000
Before-tax Income	0	200	0	200
		$\tau_k = 25\% (= \frac{50}{200})$		$\tau_a = 2.27\% (= \frac{50}{2200})$
Tax liability	0	50	22.7 (= $1000\tau_a$ )	27.3 (= $1200\tau_a$ )
After-tax return	0%	15% (= $\frac{200-50}{1000}$ )	-2.3% ( $\approx \frac{0-22.7}{1000}$ )	17.3% ( $\approx \frac{200-27}{1000}$ )
After-tax $\frac{W_m}{W_f}$		1.15 (= $1150/1000$ )		1.20 ( $\approx 1173/977$ )

# Effects of Tax Reform

Replace capital income tax with wealth tax → **Increases dispersion** in after-tax returns.

## Potential consequences:

▶ **Positive (+): Efficiency gain**

1. Use it or lose it (static): Capital is reallocated to more productive agents.
2. Behavioral savings response (dynamic): further reallocation to more productive agents.

▶ **Negative (-): Higher wealth inequality...**

but ambiguous effect on consumption inequality when wage income present.

**Conjecture:** **Positive effects will be first order** and negative effects will be second order.

We study optimal **taxation of wealth** in a **quantitative framework**:

- ▶ OLG heterogeneous agents model
- ▶ Financial frictions: collateral constraints
- ▶ Generates:
  1. Pareto tail & extreme concentration of wealth,
  2. Very fast wealth growth for super rich (1/2 of US billionaires are self made)building on power law models of inequality (Benhabib-Bisin-et al, 201X; Gabaix et al, 2016)

**Key ingredient:** **persistent heterogeneity in rates of return**

- ▶ Recent work finds evidence of such heterogeneity:  
Norway: Fagereng, Guiso, Malacrino, Pistaferri (2019); US: Smith, Yagan, Zidar, Zwick (2019).

## Preview of Key Results

When investors differ in their rates of return:

1. Capital income taxes are much more distorting than what we believed to be.
2. Switching to a wealth tax raises productivity, output, wages, and welfare.
3. In our quantitative simulations, it also reduces consumption inequality.
  - Hence, it's a policy with no equity-efficiency trade-off.
4. Gains come from reallocation, not accumulation.
  - Hence, transition path isn't painful as with capital income taxes.



1. **Model**
2. Parameterization
3. Quantitative Results
  - 3.1 Tax reform
  - 3.2 Optimal taxation
4. Robustness
5. Conclusions and Current Work

# Households

- ▶ OLG demographic structure.
- ▶ Uncertain lifetimes: individuals face mortality risk every period.
- ▶ Accidental bequests are inherited by (newborn) offspring.

## Individuals:

- ▶ Have preferences over consumption and leisure
- ▶ Make three decisions:  
consumption-savings || labor supply || entrepreneurial activity
- ▶ Two exogenous characteristics:  
 $y_{ih}$  (labor market productivity) ||  $z_{ih}$  (entrepreneurial productivity)

# 1. Labor Market Productivity $y_{ih}$

- ▶ Labor market efficiency of household  $i$  at age  $h$  is

$$\log y_{ih} = \underbrace{\kappa_h}_{\text{life cycle}} + \underbrace{\theta_i}_{\text{permanent}} + \underbrace{\eta_{ih}}_{\text{AR}(1)}$$

- ▶ Permanent component  $\theta_i$  is imperfectly inherited from parents:

$$\theta_i^{\text{child}} = \rho_\theta \theta_i^{\text{parent}} + \varepsilon_\theta$$

- ▶ Individual  $i$  produces  $x_{ih}$  units of intermediate good  $i$  using capital  $k_{ih}$ :

$$x_{ih} = z_{ih} k_{ih},$$

- Each individual is a monopolist in her variety of intermediate good.

- ▶  $z_{ih}$  has a permanent and a stochastic component:

$$z_{ih} = f\left( \underbrace{z_i^p}_{\text{perm. comp.}}, \underbrace{\mathbb{I}_{ih}}_{\text{stoch. comp.}} \right)$$

- ▶ Permanent component  $z_i^p$  is imperfectly inherited from parents:

$$\log(z_{child}^p) = \rho_z \log(z_{parent}^p) + \varepsilon_z.$$

## Entrepreneurial Productivity $z_{ih}$ : Dynamics

$\mathbb{I}_{ih}$  can take on three values:  $\mathbb{I}_{ih} \in \{H, L, \mathbf{0}\}$ :

$$z_{ih} = f(z_i^p, \mathbb{I}_{ih}) = \begin{cases} (z_i^p)^\lambda & \text{if } \mathbb{I}_{ih} = H \\ z_i^p & \text{if } \mathbb{I}_{ih} = L \\ z_{min} & \text{if } \mathbb{I}_{ih} = \mathbf{0} \end{cases} \quad \text{where } \lambda > 1$$

where  $\lambda$  is degree of **superstar productivity**.

Transition matrix:

$$\Pi_{z^s} = \begin{bmatrix} 1 - p_1 - p_2 & p_1 & p_2 \\ 0 & 1 - p_2 & p_2 \\ 0 & 0 & 1 \end{bmatrix}$$

- ▶  $p_1 = \Pr \{\text{losing superstar productivity}\}$ .
- ▶  $p_2 = \Pr \{\text{losing all productivity}\} \rightarrow$  become a passive saver.

# Competitive Final Good Producer

Final good production combines **efficiency adjusted capital** and labor:  $Y = Q^\alpha L^{1-\alpha}$

- ▶ **Efficiency-adjusted** aggregate capital:

$$Q = \left( \int (x_{ih})^\mu didh \right)^{1/\mu}, \quad \mu < 1$$

- Defines demand curve for individual entrepreneurs

- ▶ Aggregate labor supply (labor used by aggregate firm, not to produce  $x_{ih}$ ):

$$L = \int (y_{ih} \ell_{ih}) didh$$

# Bond Market & Entrepreneur's Problem

## Bond Market:

- ▶ Individuals can **lend** and **borrow** (subject to **collateral constraints**).
- ▶ Bonds in zero net supply → Interest rate  $r$  determined in equilibrium.

## Entrepreneur's Problem

- ▶ Without taxes, entrepreneur's (static!) capital choice:

$$\pi^*(a, z) = \max_{k \leq \vartheta(z) \cdot a} \{ \mathcal{R} \cdot (z \cdot k)^\mu - (r + \delta) k \}$$

- ▶ Collateral constraints: Borrowing capacity is nondecreasing in ability  $d\vartheta(z)/dz \geq 0$

## After-tax wealth:

$$\Pi(a, z; \tau) = \begin{cases} a + [ra + \pi^*(a, z)] \times (1 - \tau_k) \\ [(1 + r)a + \pi^*(a, z)] \times (1 - \tau_a) \end{cases}$$

# Budget Constraints

## Individuals:

- ▶ During working life:

$$(1 + \tau_c) \cdot c_{ih} + a'_{ih} = \Pi(a_{ih}, z_{ih}; \tau) + (1 - \tau_\ell) \cdot (wy_{ih} \ell_{ih}) \quad \text{and} \quad a'_{ih} \geq 0$$

- ▶ During retirement labor income replaced with SS pension

## Government budget balances:

- ▶ **Outlays:** Expenditure ( $G$ ) + Social Security pensions
- ▶ **Revenues:** tax on consumption ( $\tau_c$ ), labor income ( $\tau_\ell$ ), plus:
  1. tax on capital income ( $\tau_k$ ), or
  2. tax on wealth ( $\tau_a$ ).



1. Model
2. **Parameterization**
3. Quantitative Results
  - 3.1 Tax reform
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# Parameterization

- ▶ Preferences:

$$u(c, \ell) = \frac{(c^\gamma \ell^{1-\gamma})^{1-\sigma}}{1-\sigma}$$

- ▶ Dynamics of  $z_{ih}$ : Match fast wealth growth of super wealthy

- Percentage of self-made in Forbes 400 (54%, we get 50%)

examples

- ▶ We set:  $\lambda = 5$ ,  $p_1 = 0.05$ , and  $p_2 = 0.03$ .

$$\Pi_{z^s} = \begin{bmatrix} 0.92 & 0.05 & 0.03 \\ 0 & 0.97 & 0.03 \\ 0 & 0 & 1 \end{bmatrix}$$

- Robustness analysis with constant productivity:  $\lambda = 1$ ,  $p_1 = 0$ , and  $p_2 = 0$ .

## Parameters Set Outside the Model

Parameter		Value
Curvature of utility	$\sigma$	4.0
Curvature of CES aggregator of varieties	$\mu$	<b>0.90</b>
Capital share in production	$\alpha$	0.40
Depreciation rate of capital	$\delta$	0.05
Interg. persistence of invest. ability	$\rho_{z^P}$	0.10
Interg. persistence of labor efficiency	$\rho_\theta$	0.50
Persistence of labor efficiency shock	$\rho_\eta$	0.90
Std. dev. of labor efficiency shock	$\sigma_{\varepsilon_\eta}$	0.20

$\tau_k = 25\%$ ,  $\tau_\ell = 22.4\%$ , and  $\tau_c = 7.5\%$  (McDaniel, 2007)

## Calibration Targets and Outcomes

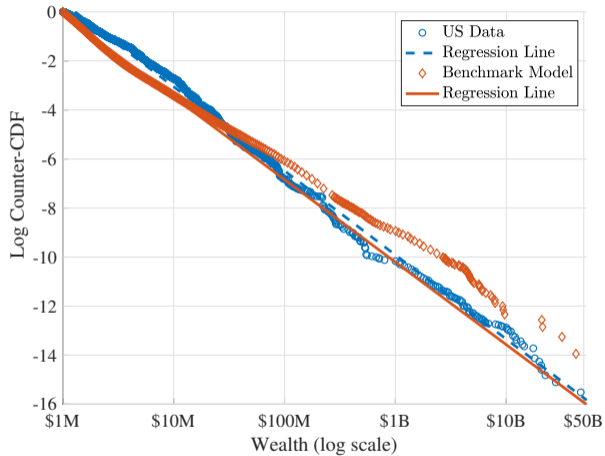
We calibrate 4 remaining parameters ( $\beta, \gamma, \sigma_{\varepsilon_{zp}}, \sigma_{\varepsilon_{\theta}}$ ) to match 4 data moments:

Parameter		Value	Moment	Data	Model
Discount factor	$\beta$	0.948	Capital/GDP	3.00	3.00
Cons. share in $U$	$\gamma$	0.46	Avg. Hours	0.40	0.40
$\sigma$ of entrep. ability	$\sigma_{\varepsilon_{zp}}$	0.072	Top 1% share	0.36	0.36
$\sigma$ of labor fix. eff.	$\sigma_{\varepsilon_{\theta}}$	0.305	$\sigma(\log(\text{Labor Earnings}))$	0.80	0.80

Untargeted moments:

Moment	Data	Model
total tax revenue/GDP	24.8%	25%
capital tax revenue/total tax revenue	28%	25%
corporate debt/GDP	126%	129%
Bequest/Wealth	1-2%	1.0%

# $\mu = 0.9$ and Pareto Tail



1. Model
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# Two Types of Experiments

1. **Tax Reform:** Replace  $\tau_k$  with  $\tau_a$  so as to
  - (a) keep government revenue constant (RN), or
  - (b) keep government budget balanced (BB).
  
2. **Optimal Taxation:** Government **maximizes utilitarian social welfare** choosing:
  - (a) linear labor income ( $\tau_\ell$ ) and capital income taxes ( $\tau_k$ ), or
  - (b) linear labor income ( $\tau_\ell$ ) and wealth taxes ( $\tau_a$ ),keeping government revenue constant.

# Revenue Neutral Tax Reform



## Tax Reform: Aggregate Variables

	Benchmark	Wealth Tax
$\tau_k$	○ 25.0%	○ 0.00
$\tau_a$	0.00	<b>1.13%</b>

Variable	% Change
$K$	<b>19.4</b>
$Q$	<b>24.8</b>
$L$	1.3
$Y$	10.1
$w$	8.7
$C$	10.0

# Reallocation of Wealth Across Agents

## Change in the share of individuals in Top x% of wealth holders by productivity type

Top x%	Entrepreneurial Productivity Groups ( $z_i^D$ Percentiles)					
	0-40	40-80	80-90	90-99	99-99.9	99.9+
1	-12.0	-13.0	-10.8	10.5	11.2	9.4
5	-8.2	-3.3	1.6	8.3	8.9	7.9
10	-6.4	-1.3	2.9	6.4	6.9	6.2
50	-2.5	0.9	1.8	1.6	1.2	1.1

## Decomposing change in wealth: Three channels

- ▶ **Use-it-or-lose-it:** Change in taxes, prices and policy rules fixed
- ▶ **GE (price) effects:** Change in taxes and prices, policy rules fixed
- ▶ **Behavioral response:** Change in policy rules in response to taxes and prices

<i>Due to:</i>	$\Delta \log K$	<i>Contrib. by <math>z_i^p</math> pctiles</i>			<i>% Change in wealth share</i>		
		0-90	90-99	99+	0-90	90-99	99+
A. Use-it-or-lose-it	14.5	3.8	4.4	6.3	-5.7	1.6	4.0
B. GE (price) effects	-13.1	-8.2	-3.2	-1.7	0.0	-0.7	0.6
C. Behavioral response	16.3	8.7	2.9	4.8	-1.4	-0.2	1.7
Total Effect (A+B+C)	17.7	4.3	4.0	9.4	-7.1	0.7	6.4

# Welfare Analysis: Two Measures

## Micro measure ( $CE_1(s)$ ):

- ▶ Individual-specific consumption-equivalent in the US benchmark that gives the same lifetime utility as in tax reform economy
- ▶  $\overline{CE}_1$ : average of  $CE_1(s)$  over the population.

## Macro measure ( $\overline{CE}_2$ ):

- ▶ Economy-wide consumption-equivalent that gives same expected lifetime utility as in tax reform economy

## Tax Reform: Average Welfare Change

	RN	BB
Average welfare difference:		
$\overline{CE}_1$	<b>7.40%</b>	5.58%
$\overline{CE}_2$	7.86%	4.71%
% with welfare gain	<b>67.8%</b>	94.8%

*Note: The welfare figures report the percentage gain in consumption-equivalent terms from each tax reform relative to the current US benchmark economy.*

	RN	BB
Average welfare difference:		
$\overline{CE}_1$	7.40%	<b>5.58%</b>

## Tax Reform: Who Gains? Who Loses?

Age	Productivity group (Percentile)					
	0-40	40-80	80-90	90-99	99-99.9	99.9+
20	<b>7.0</b>	<b>7.3</b>	<b>7.9</b>	<b>8.9</b>	<b>10.6</b>	<b>11.7</b>
21-34	6.5	6.3	6.3	6.6	7.0	6.9
35-49	5.1	4.4	3.9	3.3	1.7	0.4
50-64	2.3	1.8	1.4	0.8	-0.6	-1.7
65+	-0.2	-0.3	-0.4	-0.6	-1.2	-1.7

**Note:** Each cell reports the average of  $CE_1(\theta, z, a, h) \times 100$  within each age and productivity group

# Two Optimal Taxation Problems

The government maximizes ex ante (expected) lifetime utility of newborns by choosing

1. Linear labor income ( $\tau_\ell$ ) and capital income taxes ( $\tau_k$ ), or
2. Linear labor income ( $\tau_\ell$ ) and wealth taxes ( $\tau_a$ )

keeping government revenue constant.

- ▶ Exercise equivalent to maximizing  $\overline{CE}_2$

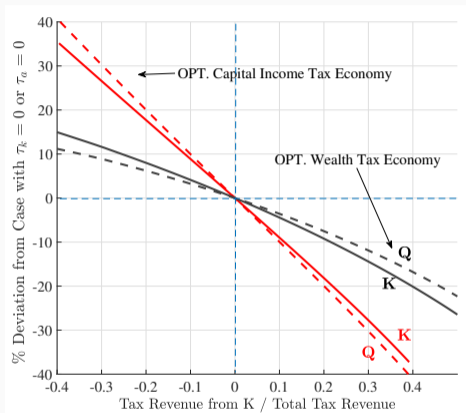
## Optimal Tax Structure and Outcomes

	$\tau_k$	$\tau_\ell$	$\tau_a$	$\bar{k}/Y$	Top 1%
Benchmark	25%	22.4%	–	3.0	0.36
Tax reform	–	22.4%	1.13%	3.25	0.46
<b>Opt. <math>\tau_k</math></b>	<b>-34.4%</b>	<b>36.0%</b>	–	<b>4.04</b>	<b>0.56</b>
<b>Opt. <math>\tau_a</math></b>	–	<b>14.1%</b>	<b>3.06%</b>	<b>2.90</b>	0.47
Opt. $\tau_a$ w/ threshold	–	14.2%	3.30%	2.86	0.47

**Note:** All experiments are revenue neutral. Threshold is 25% of av. earnings and exempts 37% of population.



# Wealth Taxes – Distortions and Misallocation



1. Wealth tax reduces Q and K **less** than capital income tax.
2. Q declines **less** than K under wealth taxes. Opposite under capital income taxes.

## Optimal Taxes: Aggregate Variables

	$\Delta K$	$\Delta Q$	$\Delta L$	$\Delta Y$	$\Delta w$	$\Delta w$ (net)	$\Delta r$	$\Delta r$ (net)
% change								
Tax reform	19.4	24.8	1.3	10.1	8.7	8.7	-0.25	-0.90
Optimal $\tau_k$	<b>69.0</b>	<b>79.8</b>	-1.2	25.5	<b>27.0</b>	<b>4.7</b>	-1.51	-0.87
Optimal $\tau_a$	<b>2.8</b>	<b>10.3</b>	3.9	6.4	<b>2.4</b>	<b>13.4</b>	0.68	-1.92
Opt. $\tau_a$ + Threshold	0.41	8.1	3.7	5.4	1.70	12.5	0.78	-2.07

## Optimal Taxes: Welfare

	$\tau_k$	$\tau_\ell$	$\tau_a$	$\overline{CE}_2$ (%)
Benchmark	25%	22.4%	-	-
Tax reform	-	22.4%	1.13%	<b>7.86</b>
Optimal $\tau_k$	-34.4%	36.0%	-	<b>6.28</b>
Optimal $\tau_a$	-	14.1%	3.06%	<b>9.61</b>
Opt. $\tau_a$ + Threshold	-	14.2%	3.30%	9.83

## Welfare: Levels vs Redistribution

	Tax Reform	Opt. $\tau_k$	Opt. $\tau_a$
$CE_2$ (NB)	<b>7.86</b>	<b>6.28</b>	<b>9.61</b>
	Consumption		
Total	8.27	5.90	11.02
Level	<b>10.01</b>	<b>21.04</b>	<b>8.28</b>
Dist.	<b>-1.58</b>	<b>-12.51</b>	<b>2.53</b>
	Leisure		
Total	-0.38	0.36	-1.27
Level	<b>-0.66</b>	<b>0.73</b>	<b>-2.21</b>
Dist.	<b>0.27</b>	<b>-0.38</b>	<b>0.76</b>

# Extension: Transition

## Optimal Tax Equilibrium with Transition

- ▶ Fix optimal capital tax level ( $\tau_k$  or  $\tau_a$ ) and solve transition to new steady state
- ▶ Adjust labor income tax ( $\tau_\ell$ ) to finance Gov. debt from deficits during transitions

	OCIT	OWT
$\tau_k$	-34.38*	0.00
$\tau_a$	0.00	3.06*
$\tau_\ell$	37.41	15.40
$\overline{CE}_2$ (newborn)	<b>-5.30</b> (6.28)	<b>7.71</b> (9.61)
$\overline{CE}_2$ (all)	<b>-3.86</b> (3.90)	<b>4.65</b> (4.79)

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# Conclusions

- ▶ Many countries currently have or have had wealth taxes:
  - France, Spain, Norway, Switzerland, Italy, Denmark, Germany, Finland, Sweden, Colombia, among others.
- ▶ However, the **rationale for wealth taxes are often vague**:
  - fairness, reducing inequality, etc...
  - and not studied formally
- ▶ Here, we are proposing **a case for wealth taxes based on efficiency** (and distributional benefits) and quantitatively evaluating its impact.



# Wealth tax has opposite implications of capital income tax

**Tax reform from  $\tau_k$  to  $\tau_a$ :** Substantial welfare gains

- ▶ **Reallocates capital:** less productive wealthy  $\rightarrow$  more productive agents
- ▶ Gives the right incentives to the right people to save
- ▶ Increases output, consumption, and wages

**Optimal taxes:** Welfare gain substantially larger under wealth taxes

- ▶ Capital income taxes ( $\tau_k$ ): negative or small, gains go away with transition
- ▶ Wealth taxes ( $\tau_a$ ): positive and large, act through reallocation not accumulation

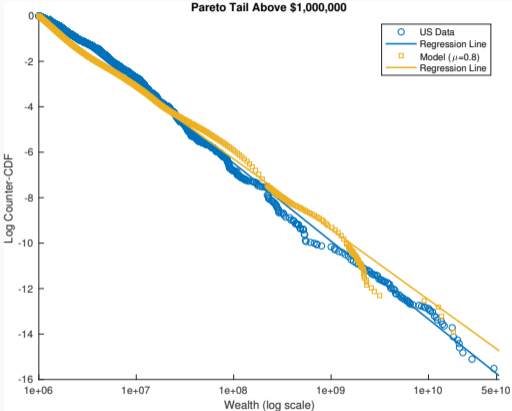
# Current and Future Work

1. Add optimal **consumption taxes**.
2. Are **global wealth taxes** necessary?
  - More productive agents prefer wealth tax over capital income tax
3. Alternative modeling of **entrepreneur's labor input**
  - How much of the return to entrepreneurship comes from human capital?

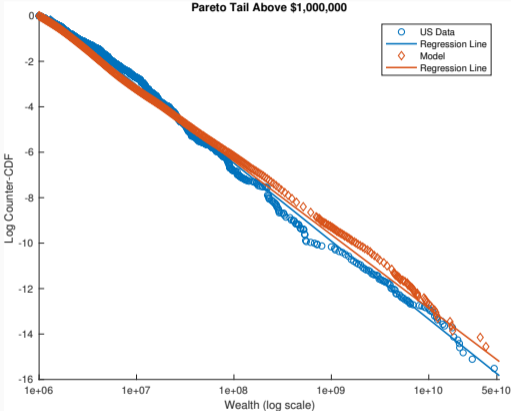
**Thanks!**

# Appendix

# Pareto Tail with Modified Models



(a)  $\mu = 0.8$



(b) Measuring Wealth in Present Values

# Reallocation of Wealth Across Agents

	Percentiles of Return Distribution (%)				
	P10	P50	P90	P95	P99
	<b>Before Tax</b>				
Benchmark	2.00	2.00	17.28	22.35	42.36
Wealth tax	1.74	1.74	14.62	19.04	36.91
	<b>After Tax</b>				
Benchmark	1.50	1.50	12.96	16.76	31.77
Wealth tax	0.59	0.59	13.32	17.69	35.35

# Wealth Concentration by Assets

**Table 1:** Wealth Concentration by Asset Type

	<i>Stocks w/o pensions</i>	<i>All stocks</i>	<i>Non-equity financial</i>	<i>Housing equity</i>	<i>Net Worth</i>
Top 0.5%	41.4	37.0	24.2	10.2	25.6
Top 1%	53.2	47.7	32.0	14.8	34.0
Top 10%	91.1	86.1	72.1	51.7	68.7
Bottom 90%	8.9	13.9	27.9	49.3	31.3
<b>Gini Coefficients</b>					
	<i>Financial Wealth</i>			<i>Net Worth</i>	
	0.91			0.82	

Source: Poterba (2000) and Wolff (2000)

# Evolution of Net Worth Among Forbes 400

../../../../2016/UBC\_SF/Forbes\_figures/F400\_age.eps

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# Information on Billionaires

Name	Calendar Year			
	80s	90s	00s	10s
Warren Buffett	44.37	18.57	0.02	5.81
Michael Dell		87.94	-5.58	2.97
Larry Ellison	54.09	31.31	4.90	8.06
Bill Gates	51.94	48.06	-7.54	5.46
Elon Musk				107.57
Larry Page			69.67	11.96
Mark Zuckerberg			33.81	62.24

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# Welfare Analysis: Two Measures

**Notation:**  $\mathbf{s}$  state vector ||  $V_0$  and  $\mathbb{V}_0$  be lifetime value functions in benchmark (US) and counterfactual economies ||  $\Gamma$  be the distribution of  $\mathbf{s}$ .

**Micro measure ( $CE_1(\mathbf{s})$ ):**

- ▶ Compute individual-specific consumption equivalent welfare and integrate:

$$V_0((1 + CE_1(\mathbf{s})) c_{US}^*(\mathbf{s}), l_{US}^*(\mathbf{s})) = \mathbb{V}_0(c(\mathbf{s}), l(\mathbf{s}))$$

$$\overline{CE}_1 \equiv \sum_{\mathbf{s}} \Gamma_{US}(\mathbf{s}) \times CE_1(\mathbf{s})$$

**Macro measure ( $\overline{CE}_2$ ):**

- ▶ Fixed proportional consumption transfer to all Individual all individuals:

$$\sum_{\mathbf{s}} \Gamma_{US}(\mathbf{s}) \times V_0((1 + \overline{CE}_2) c_{US}^*(\mathbf{s}), l_{US}^*(\mathbf{s})) = \sum_{\mathbf{s}} \Gamma(\mathbf{s}) \times \mathbb{V}_0(c(\mathbf{s}), l(\mathbf{s})).$$

# Welfare Gain Decomposition

Decompose welfare into consumption ( $CE_C$ ) and leisure gain ( $CE_L$ ):

$$1 + CE = (1 + CE_C)(1 + CE_L)$$

►  $CE_C$  is given by:

$$V_0((1 + CE_C(\mathbf{s}))c_{US}^*(\mathbf{s}), l_{US}^*(\mathbf{s})) = \tilde{V}_0(c(\mathbf{s}), l_{US}^*(\mathbf{s}))$$

■  $CE_C$  can be decomposed into level ( $CE_{\bar{c}}$ ) and distribution ( $CE_{\sigma_c}$ )

$$V_0((1 + CE_{\bar{c}}(\mathbf{s}))c_{US}^*(\mathbf{s}), l_{US}^*(\mathbf{s})) = \hat{V}_0(\hat{c}(\mathbf{s}), l_{US}^*(\mathbf{s}))$$

where  $\hat{c}(\mathbf{s}) = c(\mathbf{s}) \frac{\bar{c}}{c_{US}^*}$  and

$$\hat{V}_0((1 + CE_{\sigma_c})\hat{c}(\mathbf{s}), l_{US}^*(\mathbf{s})) = \tilde{V}_0(c(\mathbf{s}), l_{US}^*(\mathbf{s}))$$

►  $CE_L$  is given by

$$V_0((1 + CE_L(\mathbf{s}))c_{US}^*(\mathbf{s}), l(\mathbf{s})) = \tilde{V}_0(c_{US}^*(\mathbf{s}), l(\mathbf{s}))$$

■ Similar decomposition applies to leisure.

# Political Support for Optimal Capital Taxes

Age	Productivity group (Percentile)						
	0-40	40-80	80-90	90-99	99-99.9	99.9-99.99	99.99+
20	95.4	98.6	99.3	99.6	99.8	99.8	100.0
21-34	96.3	97.7	97.7	97.3	96.0	94.9	92.3
35-49	91.7	92.8	91.1	87.8	80.3	74.5	63.7
50-64	74.2	76.2	73.8	69.4	60.3	53.8	43.8
65+	13.8	18.6	18.7	18.2	16.6	15.2	13.0

**Note:** Each cell reports the share of agents in each category (age - productivity) with positive welfare gain ( $CE_1(\theta, z, a, h) > 0$ ).

# Political Support for Optimal Wealth Taxes

Age	Productivity group (Percentile)						
	0-40	40-80	80-90	90-99	99-99.9	99.9-99.99	99.99+
20	94.5	93.1	93.3	94.6	95.8	96.1	95.8
21-34	95.7	92.6	90.5	88.8	84.2	79.4	67.0
35-49	91.3	82.8	76.5	68.2	53.6	44.6	34.0
50-64	72.6	62.9	56.1	49.4	39.8	34.5	27.2
65+	2.1	2.3	1.8	1.4	0.9	0.7	0.4

**Note:** Each cell reports the share of agents in each category (age - productivity) with positive welfare gain ( $CE_1(\theta, z, a, h) > 0$ ).

## Political Support for Wealth Taxes with Threshold

Age	Productivity group (Percentile)						
	0-40	40-80	80-90	90-99	99-99.9	99.9-99.99	99.99+
20	94.5	93.1	93.3	94.6	95.8	95.9	96.0
21-34	95.6	92.4	90.4	88.5	83.8	77.6	78.9
35-49	91.1	82.4	76.0	67.8	53.2	43.3	44.3
50-64	76.4	66.7	59.6	52.5	42.3	35.8	36.6
65+	75.9	68.6	63.7	57.9	48.7	42.1	42.9

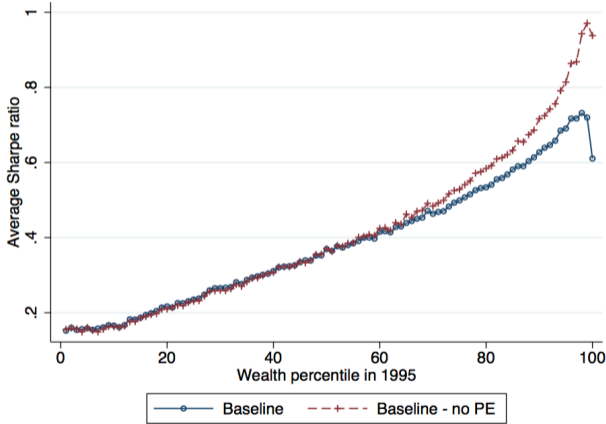
**Note:** Each cell reports the share of agents in each category (age - productivity) with positive welfare gain ( $CE_1(\theta, z, a, h) > 0$ ).

## How Much Inequality in Aiyagari-Style Models?

Parametrization:	U.S. Data	Gaussian	GKOS benchmark
		$\rho = 0.985, \sigma^2 = 0.0234$	Rich process
Gini	0.85	0.58	0.66
<b>Top 0.1%</b>	<b>14.8%</b>	<b>1.1%</b>	<b>2.2%</b>
<b>Frac &gt; \$10M</b>	<b>0.4–0.5%</b>	$\approx 0$	<b>0.02%</b>
Top 1%	35.5%	7.0%	9.2%
Top 10%	75.0%	37.9%	41.6%
Top 20%	87.0%	48.2%	52.8%

# Return Heterogeneity in Norway

Figure 8. The Sharpe ratio and the level of wealth



Source: Fagereng, Guiso, Malacrino, and Pistaferri (2016)